

1. Let

$$f(x) = \begin{cases} 0 & x \in (-\infty, 0) \cup (4, \infty) \\ C(-4x^3 + 16x^2) & x \in [0, 4]. \end{cases}$$

- (a) Verify that  $f$  is nonnegative.
- (b) Find a value for  $C$  such that  $f$  is a valid probability density function.